

A MODEL OF SYNOVIAL FLUID LUBRICANT COMPOSITION IN NORMAL AND INJURED JOINTS

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Abstract

The synovial fluid (SF) of joints normally functions as a biological lubricant, providing low-friction and low-wear properties to articulating cartilage surfaces through the putative contributions of proteoglycan 4 (PRG4), hyaluronic acid (HA), and surface active phospholipids (SAPL). These lubricants are secreted by chondrocytes in articular cartilage and synoviocytes in synovium, and concentrated in the synovial space by the semi-permeable synovial lining. A deficiency in this lubricating system may contribute to the erosion of articulating cartilage surfaces in conditions of arthritis. A quantitative intercompartmental model was developed to predict *in vivo* SF lubricant concentration in the human knee joint. The model consists of a SF compartment that (a) is lined by cells of appropriate types, (b) is bound by a semi-permeable membrane, and (c) contains factors that regulate lubricant secretion. Lubricant concentration was predicted with different chemical regulators of chondrocyte and synoviocyte secretion, and also with therapeutic interventions of joint lavage and HA injection. The model predicted steady-state lubricant concentrations that were within physiologically observed ranges, and which were markedly altered with chemical regulation. The model also predicted that when starting from a zero lubricant concentration after joint lavage, PRG4 reaches steady-state concentration ~10-40 times faster than HA. Additionally, analysis of the clearance rate of HA after therapeutic injection into SF predicted that the majority of HA leaves the joint after ~1-2 days. This quantitative intercompartmental model allows integration of biophysical processes to identify both environmental factors and clinical therapies that affect SF lubricant composition in whole joints.

Keywords: synovial fluid, proteoglycan 4, hyaluronic acid, permeability, cartilage, synovium, lavage, HA injection

Introduction

The synovial fluid (SF) of natural joints normally functions as a biological lubricant as well as a biochemical pool through which nutrients and regulatory cytokines traverse. SF contains molecules that provide low-friction and low-wear properties to articulating cartilage surfaces. Molecules postulated to play a key role, alone or in combination, in lubrication are proteoglycan 4 (PRG4) (Swann *et al.*, 1985) present in SF at a concentration of 0.05-0.35 mg/ml (Schmid *et al.*, 2001a), hyaluronan (HA) (Ogston and Stanier, 1953) at 1-4 mg/ml (Mazzucco *et al.*, 2004), and surface-active phospholipids (SAPL) (Schwarz and Hills, 1998) at 0.1 mg/ml (Mazzucco *et al.*, 2004). Synoviocytes secrete PRG4 (Jay *et al.*, 2000; Schumacher *et al.*, 1999) and are the major source of SAPL (Dobbie *et al.*, 1995; Hills and Crawford, 2003; Schwarz and Hills, 1996), as well as HA (Haubeck *et al.*, 1995; Momberger *et al.*, 2005), in SF. Other cells also secrete PRG4, including chondrocytes in the superficial layer of articular cartilage (Schmid *et al.*, 2001b; Schumacher *et al.*, 1994) and, to a much lesser extent, cells in the meniscus (Schumacher *et al.*, 2005).

As a biochemical depot, SF is an ultrafiltrate of plasma that is concentrated by virtue of its filtration through the synovial membrane. The synovium is a thin lining (~50 μ m in humans) comprised of tissue macrophage A cells, fibroblast-like B cells (Athanasou and Quinn, 1991; Revell, 1989; Wilkinson *et al.*, 1992), and fenestrated capillaries (Knight and Levick, 1984). It is backed by a thicker layer (~100 μ m) of loose connective tissue called the subsynovium (SUB) that includes an extensive system of lymphatics for clearance of transported molecules. The cells in the synovium form a discontinuous layer separated by intercellular gaps of several microns in width (Knight and Levick, 1984; McDonald and Levick, 1988). The extracellular matrix in these gaps contains collagen types I, III, and V (Ashhurst *et al.*, 1991; Rittig *et al.*, 1992), hyaluronan (Worrall *et al.*, 1991), chondroitin sulphate (Price *et al.*, 1996; Worrall *et al.*, 1994), biglycan and decorin proteoglycans (Coleman *et al.*, 1998a), and fibronectin (Poli *et al.*, 2004). The synovial matrix provides the permeable pathway through which exchange of molecules occurs (Levick, 1994), but also offers sufficient outflow resistance (Coleman *et al.*, 1998a; Scott *et al.*, 1998) to retain large solutes of SF within the joint cavity. Together, the appropriate reflection of secreted lubricants by the synovial membrane and the appropriate lubricant secretion by cells are necessary for development of a mechanically functional SF.

The mechanobiology of joints and SF constitutes a complex, low-friction, low-wear system that is normally in homeostasis. However, in arthritis, injury, and artificial

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joint failure, there is increased friction between the articulating surfaces and concomitant erosion of the load bearing elements (Buckwalter and Mankin, 1997). This increase in friction is associated with altered SF composition. Specifically, the SF PRG4 concentration decreases following acute injury, as does the friction-lowering property of such SF (Elsaid *et al.*, 2005), while PRG4 concentration increases in patients undergoing arthrocentesis procedures (Schmid *et al.*, 2001a). HA (Belcher *et al.*, 1997) and SAPL (Rabinowitz *et al.*, 1984) also exhibit decreased concentrations in osteoarthritis, and HA is also decreased with failure of artificial joints (Mazzucco *et al.*, 2004). The mechanisms by which altered SF lubricant composition occur are unknown.

Joint injury and arthritis may additionally result in dramatic changes in the concentration of some cytokines in SF (Bertone *et al.*, 2001; Cameron *et al.*, 1994; Fahlgren *et al.*, 2001; Fava *et al.*, 1989; Moos *et al.*, 1999; Okazaki *et al.*, 2001; Wei and Messner, 1998). A complex milieu of regulatory cytokines exists in SF, including TGF- β , IGF-1, TNF- α , IL-1, and IL-6 (Fava *et al.*, 1989; Kaneyama *et al.*, 2005; Schalkwijk *et al.*, 1989; Van Obberghen-Schilling *et al.*, 1988; Wei and Messner, 1998). The cytokines TGF- β and IL-1 can have significant effects on secretion of lubricants by both chondrocytes and synoviocytes. IL-1 downregulates PRG4 secretion by chondrocytes, while TGF- β upregulates PRG4 secretion (Flannery *et al.*, 1999; Schmidt *et al.*, 2005). Additionally, both TGF- β and IL-1 result in increased HA secretion by synoviocytes (Haubeck *et al.*, 1995; Momberger *et al.*, 2005). Thus, the changing chemical environment with injury and arthritis may have significant effects on lubricant secretion by cells, and, consequently, SF lubricant composition.

A variety of treatments have been developed to alter biologically the synovial joint environment in injury and arthritis. Some pharmaceutical agents are capable of reducing pain and inflammation (Furst, 2004; Moreland, 2004). HA injections have been purported to affect the biology of the joint in order to restore the viscosity and protective functions of the synovial fluid (Moreland, 2003; Tehranzadeh *et al.*, 2005). Therapeutic joint lavage has been used to cleanse the joint of cartilage degradation products, proinflammatory cells, and destructive enzymes associated with arthritis (Ayril, 2005), and can be performed alone or in combination with anti-inflammatory steroids (Frias *et al.*, 2004; Tanaka *et al.*, 2006). These treatments have not specifically targeted restoration of lubrication in joints, and treatment effects on SF lubricant composition have not yet been examined.

The whole synovial joint, including cartilage, synovium and SF (Fig. 1), presents complexities that make it difficult to measure continuously the *in vivo* SF lubricant composition, and also the main determinants of dynamics in this composition. General models of fluid flow and solute transport through a matrix (reviewed in (Curry, 1984; Levick, 1987)) have been developed, and extensive analysis of the synovium structure has been performed to obtain values for functional parameters that control its transport properties (Levick, 1994; Levick and McDonald, 1989a; Levick and McDonald, 1989b; Price *et al.*, 1996;

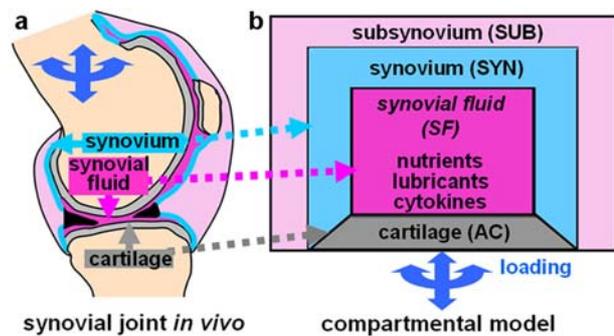


Figure 1. (a) Synovial joints are generally composed of cartilage, synovium, and SF, (b) modelled by communicating compartments in which chemical and mechanical factors regulate lubricant secretion.

Price *et al.*, 1995; Sabaratnam *et al.*, 2005; Scott *et al.*, 2003). Knowledge of the structure of synovium, along with related published data, has been applied to the models of fluid and solute transport to specifically model the flow of albumin from synovial capillaries into SF and out through the synovial membrane (Levick, 1994). Additionally, the concept of combining the theory of mass balance with the data on fluid and solute transport through the synovium has been introduced as an approach for determining the concentration of a molecule in SF, such as a lubricant (Levick, 1998).

Thus, the objective of this study was to develop a mathematical model to analyze lubricant composition in SF of whole human knee joints, expanding upon the approaches taken in previous studies and utilizing relevant published functional parameters. The model was applied to determine theoretically (1) the steady-state lubricant concentration in SF under normal and altered chemical environments in the synovial joint that may occur with injury and disease, (2) the kinetics associated with attaining these steady-state concentrations from a zero starting concentration after simulated joint lavage, and (3) the clearance rate of HA from the joint after simulated therapeutic HA injection. The validity of the model was assessed by comparison of the lubricant concentrations predicted at steady-state with those observed *in vivo*.

Model

Model Overview

The model consists of a SF compartment surrounded by articular cartilage and a semi-permeable synovial membrane that separates the SF from an underlying subsynovium (SUB) compartment (Fig. 2). Lubricants are secreted into the SF by chondrocytes in articular cartilage (AC) and synoviocytes in the synovium (SYN). Some lubricants are lost from the SF by either degradation or flux through the membrane into the SUB; however, the synovium offers sufficient outflow resistance to retain a large pool of lubricant macromolecules in the SF. Transient accumulation of lubricants exists in the SF compartment until the system reaches a steady-state lubricant composition. A complete list of variables and parameters included in the model are shown in Table 1.

Governing Equations

The rate of change in mass of lubricant i (i =PRG4, HA, or SAPL) that has a concentration of c_i^{SF} in a SF volume of V^{SF} is assumed to depend on the secretion rate of i by AC (r_i^{AC}) and SYN (r_i^{SYN}) of areas A^{AC} and A^{SYN} , the degradation rate of i in SF (d_i), and the flux of i across the synovial membrane area (J_i^{SYN}). All parameters are also a function of time, t , and the environment, which is described by the parameter α and includes chemical and mechanical factors.

A mass balance applied to the SF compartment results in:

$$\frac{\partial[V^{SF}(t,\alpha) \cdot c_i^{SF}(t,\alpha)]}{\partial t} = r_i^{SYN}(t,\alpha) \cdot A^{SYN}(t,\alpha) + r_i^{AC}(t,\alpha) \cdot A^{AC}(t,\alpha) - d_i(t,\alpha) \cdot V^{SF}(t,\alpha) - J_i^{SYN}(t,\alpha) \quad (1)$$

The degradation rate of i (d_i) is dependent upon the concentration and activity of degradative enzyme in SF. For example, the protein PRG4 may be targeted by various enzymes, and in particular has been shown to be degraded by elastase (Elsaid *et al.*, 2005). As shown by that study in a rabbit knee model of acute injury, injured SF had an elastase activity level of 1-4 μ units/ml, or about 0.2-0.6 pg/ml of elastase (1 mg = \sim 6.8 units) Application of 7 μ g of elastase to 5 μ g of PRG4 resulted in complete degradation of PRG4 within 2-6 hours. Thus, d_i can be of the form:

$$d_i(t,\alpha) = X(t,\alpha) \cdot Y(t,\alpha) \cdot c_i^{SF}(t,\alpha) \cdot V^{SF}(t,\alpha) \quad (2)$$

where X is the ratio of concentration of degradative enzyme

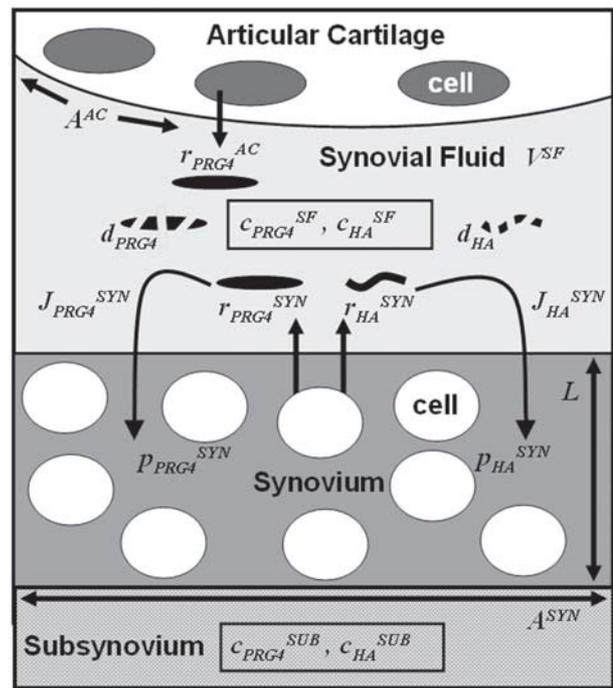


Figure 2. Schematic of synovial fluid composition model. Cartilage and synovium form a compartment around the synovial fluid, where lubricants secreted by the chondrocytes and synoviocytes are retained by the semi-permeable synovium. See Table 1 for a complete list of variables.

Table 1 List of variables and parameters

Variable or parameter	Units	Description
i		PRG4, HA
c_i^{SF}	mg/ml	Concentration of i in synovial fluid
c_i^{SUB}	mg/ml	Concentration of i in subsynovium
J_i^{SYN}	mg/s	Total flux of i through membrane area
$J_{i,diff}^{SYN}$	mg/s	Flux of i due to diffusion
$J_{i,conv}^{SYN}$	mg/s	Flux of i due to fluid convection
J_v^{SYN}	ml/s	Fluid flow rate out of the synovium
p_i^{SYN}	cm/s	Permeability of i through synovium
p_i^{INT}	cm/s	Permeability of i through interstitial space, or extracellular space
$\Delta\pi_i$	cm H ₂ O	Osmotic pressure diff. of SF and SUB
ΔP^{SYN}	cm H ₂ O	Hydrostatic pressure diff. of SF and SUB
k_i	cm/(s \cdot cm H ₂ O)	Hydraulic conductance of synovium
r_i^{SYN}	mg/(cm ² \cdot s)	Secretion rate of i by synoviocytes (SYN)
r_i^{AC}	mg/(cm ² \cdot s)	Secretion rate of i by articular cartilage (AC)
d_i	mg/s	Degradation rate of i in synovial fluid
A^{SYN}	cm ²	Area of synovial membrane
A^{AC}	cm ²	Area of cartilage surfaces
L	cm	Membrane thickness
t	s	Time
α		Environmental factor
V^{SF}	ml	Volume of synovial fluid
D_i	cm ² /s	Diffusion coefficient of i in free solution
D_i^{SYN}	cm ² /s	Restricted diffusion coeff. of i in synovium
ϕ_i		Partition coefficient of i for synovium
σ_i		Reflection coefficient of i for synovium
θ_{cell}		Volume fraction of cells in synovium
θ_{col}		Volume fraction of collagen in synovium
θ_{GAG}		Polymer volume fraction in GAG matrix
ρ_i	mg/ml	Density of i
a_{GAG}	nm	Radius of GAG chains in synovium
a_i	nm	Radius of i
ζ_{col}		Tortuosity due to collagen fibrils
ζ_{cell}		Tortuosity due to cells

in SF to the concentration of lubricant in SF, and Y is the mass of substrate degraded per mass of enzyme per unit time. A similar analysis can be performed for other degradative enzymes that target PRG4, and also for enzymes present in SF that degrade HA, such as hyaluronidase.

The flux of lubricants (J_i^{SYN}) across the membrane is a sum of the solute flux due to diffusion ($J_{i,diff}^{SYN}$) and the solute flux due to convective fluid flow ($J_{i,conv}^{SYN}$):

$$J_i^{SYN} = J_{i,diff}^{SYN} + J_{i,conv}^{SYN} \quad (3)$$

$J_{i,diff}^{SYN}$ is dependent upon the permeability (p_i^{SYN}) and area (A^{SYN}) of the synovial membrane and the concentration gradient between the *SF* and *SUB* compartments:

$$J_{i,diff}^{SYN}(t, \alpha) = p_i^{SYN}(t, \alpha) \cdot [c_i^{SF}(t, \alpha) - c_i^{SUB}(t, \alpha)] \cdot A^{SYN}(t, \alpha) \quad (4)$$

$J_{i,conv}^{SYN}$ is dependent upon the fluid flow out of the membrane (J_v^{SYN}), the reflection coefficient of the membrane (σ_i), and the concentration of i in SF (c_i^{SF}) (Curry, 1984; Patlak *et al.*, 1963):

$$J_{i,conv}^{SYN} = J_v^{SYN} (1 - \sigma_i) \cdot c_i^{SF} \quad (5)$$

J_v^{SYN} can be described by the following expression for fluid flow across a leaky membrane (Kedem and Katchalsky, 1958):

$$J_v^{SYN} = k[\Delta P^{SYN}(t, \alpha) - \sigma_i(t, \alpha)\Delta\pi_i(t, \alpha)] \cdot A^{SYN}(t, \alpha) \quad (6)$$

where ΔP^{SYN} is the hydrostatic pressure difference and $\Delta\pi_i$ is the osmotic pressure difference between *SF* and *SUB* compartments, respectively, and k is the hydraulic conductance of the synovium.

Membrane Permeability

Lubricant transport through the synovium occurs around the spaces, or volume fractions, occupied by synoviocytes (θ_{cell}) and collagen fibrils (θ_{col}), and around the polymer volume fraction of glycosaminoglycans (θ_{GAG}), and is further limited by the tortuosity of the pathway imposed by the cells (ζ_{cell}) and collagen fibrils (ζ_{col}) (Levick, 1994). Thus, there is restricted diffusion of lubricants within the synovium compared to diffusion in free solution. The restricted diffusion coefficient (D_i^{SYN}) for a globular solute within the GAG matrix of synovium is related to the diffusion coefficient in free solution (D_i), θ_{GAG} , the radius of GAG chains (a_{GAG}), and the effective radius of the solute (a_i) (Ogston *et al.*, 1973):

$$D_i^{SYN}(t, \alpha) = D_i \cdot e^{\{-\sqrt{\theta_{GAG}(t, \alpha)} \cdot (1 + \frac{a_i}{a_{GAG}})\}} \quad (7)$$

The a_i can be taken as the Stokes-Einstein equivalent radius of a solute, estimated from its molecular weight (MW) and density (ρ), according to the following, where N_a is Avogadro's number (Tanford, 1961):

$$a_i = \left(\frac{3 \cdot MW}{4 \cdot \pi \cdot \rho \cdot N_a} \right)^{1/3} \quad (8)$$

The permeability associated with the interstitial, or extracellular, space (p_i^{INT}) is a function of the restricted diffusion coefficient of the lubricant in the matrix (D_i^{SYN}), the partition coefficient (ϕ_i), the volume fraction (θ_{col}) and tortuosity (ζ_{col}) of the impenetrable collagen matrix components, and the thickness of the membrane (L) (Levick, 1994):

$$p_i^{INT}(t, \alpha) = \frac{D_i^{SYN}(t, \alpha) \cdot \phi_i(t, \alpha) \cdot [1 - \theta_{col}(t, \alpha)] \cdot \zeta_{col}(t, \alpha)}{L} \quad (9)$$

The ϕ_i of the lubricant in the matrix represents the ratio of the available solute space to the space occupied by the GAGs. The fractional space available to the solute (K_{AV}) is given by the Ogston relation (Ogston *et al.*, 1973).

$$K_{AV}(t, \alpha) = e^{\{-\frac{\theta_{GAG}(t, \alpha)}{a_{GAG}^2} (a_{GAG} + a_i)^2\}} \quad (10)$$

The ϕ_i is related to K_{AV} by the following (Curry, 1984):

$$\phi_i(t, \alpha) = \frac{K_{AV}(t, \alpha)}{e^{-\theta_{GAG}}} \quad (11)$$

Finally, the permeability of the entire synovium (p_i^{SYN}) to the lubricant i is a function of the interstitial permeability (p_i^{INT}), and also the volume fraction (θ_{cell}) and tortuosity (ζ_{cell}) imposed by the impenetrable synoviocytes in the membrane (Levick, 1994):

$$p_i^{SYN}(t, \alpha) = p_i^{INT}(t, \alpha) \cdot [1 - \theta_{cell}(t, \alpha)] \cdot \zeta_{cell}(t, \alpha) \quad (12)$$

Non-dimensional equations

The governing equations of the model can be non-dimensionalized by defining non-dimensional concentration ($c_i'^{SF}$), secretion rates ($r_i'^{SYN}$, $r_i'^{AC}$), degradation rate (d_i') and time (t'):

$$c_i'^{SF} = \frac{c_i^{SF}}{c_{i,basal}^{SF}} \quad (13)$$

$$r_i'^{SYN} = \frac{r_i^{SYN}}{r_{i,basal}^{SYN}} \quad (14)$$

$$r_i'^{AC} = \frac{r_i^{AC}}{r_{i,basal}^{AC}} \quad (15)$$

$$d_i' = \frac{d_i}{d_{i,basal}} \quad (16)$$

$$t' = \frac{t}{\tau_i} \quad (17)$$

After substitution and simplification, a non-dimensional mass balance governing equation results:

$$\frac{\partial c_i^{SF}}{\partial t'} = k_1 r_i^{SYN} + k_2 r_i^{AC} - k_3 d_i' - c_i^{SF} \quad (18)$$

The non-dimensional parameters, k_1 , k_2 , k_3 , and the dimensional τ_i are defined below:

$$k_1 = \frac{r_{i,basal}^{SYN}}{p_i^{SYN} c_{i,basal}^{SF}} \quad (19)$$

$$k_2 = \frac{A^{AC} r_{i,basal}^{AC}}{A^{SYN} p_i^{SYN} c_{i,basal}^{SF}} \quad (20)$$

$$k_3 = \frac{d_{i,basal}}{A^{SYN} p_i^{SYN} c_{i,basal}^{SF}} \quad (21)$$

$$\tau_i = \frac{V^{SF}}{p_i^{SYN} A^{SYN}} \quad (22)$$

Model Assumptions

General assumptions. It is assumed that the only parameters in the model that are altered with changes in the chemical environment (i.e. are a function of a) are the lubricant secretion rates and the dependent lubricant concentration. It is also assumed that the concentration of lubricants in the SUB compartment is zero for all situations, as transported fluid and solutes drain away *via* the system of lymphatics along intermuscular connective tissue planes (Jensen *et al.*, 1993; Levick, 1980a; Levick, 1980b).

$$c_i^{SUB}(t, \alpha) = 0 \quad (23)$$

SF volume is kept in a steady-state, as the filtration of fluid across the capillary wall into SF occurs at a rate equal to that of lymph flow (Levick, 1987). It is also assumed that the degradation of lubricants is negligible compared to cellular secretion rates:

$$d_i(t, \alpha) = 0 \quad (24)$$

Additionally, the flux of lubricants due to fluid convection is also considered negligible compared to the flux due to diffusion, as the ratio of convective transport of solute to diffusive transport of solute was estimated for albumin to be $\ll 1$ (McDonald and Levick, 1993):

$$J_{i,conv}(t, \alpha) = 0 \quad (25)$$

Further support for this assumption comes from the fact that convective fluid flow out of the joint cavity may be attenuated by SF osmotic pressure at high lubricant concentrations, and also by a concentration polarization phenomenon for large molecules in SF such as HA (McDonald and Levick, 1992; Sabaratnam *et al.*, 2004; Scott *et al.*, 2000).

Case 1: Steady-state. The concentration of lubricants at steady-state will not change with time:

$$\frac{\partial c_i^{SF}}{\partial t}(t = \infty, \alpha) = 0 \quad (26)$$

Case 2: Joint lavage. After joint lavage, the concentration of lubricants in the SF will be effectively reduced to zero:

$$c_i^{SF}(t = 0, \alpha) = 0 \quad (27)$$

The secretion rates with no chemical stimulation will be considered to be basal levels. Also, the volume of SF will be unaffected by the lavage procedure as any volume of fluid that remains in the joint and exceeds normal SF volume will be removed quickly. The transynovial flow rate of water is normally ~ 5 - 10 $\mu\text{l}/\text{min}$ at an intraarticular pressure of ~ 2 cmH_2O (flexed knee joint), but under raised intraarticular pressures of ~ 20 cmH_2O (chronic joint effusion) that occur with large increases in SF volume, is ~ 20 - 40 $\mu\text{l}/\text{min}$ (Coleman *et al.*, 1998b; Scott *et al.*, 1997). Thus, the SF volume of ~ 1 ml in normal human knee joints turns over in ~ 1 - 2 hrs, and portions of volumes in excess of this would likely equilibrate in < 1 hr.

Case 3: HA injection. Prior to the injection, the concentration of HA in SF will be equal to that achieved at steady-state:

$$c_{HA}^{SF}(t = 0^-, \alpha) = c_{HA}^{SF}(t = \infty, \alpha) \quad (28)$$

HA injections are generally on the order of 20 mg (Tehranzadeh *et al.*, 2005), and this will represent the bolus of HA introduced into the joint.

$$c_{HA}^{SF}(t = 0^+, \alpha) = c_{HA}^{SF}(t = 0^-, \alpha) + \frac{20\text{mg}}{V^{SF}} \quad (29)$$

The volume of SF will also be unaffected by this procedure due to the relatively high transynovial flow rate of water, particularly at raised intraarticular pressures and volumes. With a flow rate of ~ 20 - 40 $\mu\text{l}/\text{min}$ (Coleman *et al.*, 1998b; Scott *et al.*, 1997), a typical injection of 2 ml buffer solution would drain in ~ 1 - 2 hr.

Model Parameters

Values for parameters used in the model are based on published values in the literature. The properties of cartilage, synovium, and synovial fluid utilized in the model include cartilage and synovium surface area, synovial fluid volume, and organization of the synovium relating to transynovial transport. The total surface area in the human knee joint is 121 cm^2 for cartilage (Eckstein *et al.*, 2001) and 277 cm^2 for synovium (Davies, 1946), and the synovial fluid volume enclosed by these surfaces is 1.1 ml (Ropes *et al.*, 1940). The synovium, which is 50 μm thick in humans (Price *et al.*, 1995), has a cell volume fraction varying from 0.42 at the surface to 0.67 in deeper layers and a tortuosity due to the cells of 0.69 (Levick and McDonald, 1989a; Levick and McDonald, 1989b). The

volume fraction due to collagen is 0.2 (Levick, 1994) and the tortuosity is 0.70 (Maroudas, 1970; Sullivan and Hertel, 1942). The portion of synovium through which lubricants travel contains GAG chains with radii of 0.56 nm (Ogston *et al.*, 1973) and a volume fraction of 0.0075 (Sabaratnam *et al.*, 2005; Scott *et al.*, 2003).

The molecular weight forms of PRG4 that have been isolated from SF and cartilage exist in the range of 220 kDa (Swann *et al.*, 1977) to 345 kDa (Schumacher *et al.*, 1994), while HA exists in the range of 2000-6000 kDa (Fraser *et al.*, 1997). The mass density for both PRG4 and HA is 1.45 g/ml (Mahlbacher *et al.*, 1992; Mason *et al.*, 1982; Swann *et al.*, 1981). These parameters were used together to calculate a range of PRG4 and HA radii, assuming the idealized case that they exist in SF as globular solutes.

Diffusion coefficients have been determined for PRG4 and HA in free solution, and are 1.11×10^{-7} cm²/s (Swann *et al.*, 1981) and 9.8×10^{-8} cm²/s (Lu *et al.*, 2005), respectively. These free diffusion coefficients were used with the above parameter values of tissue and lubricant properties to calculate restricted diffusion and also permeability of lubricants through synovium.

Secretion rates used in the model depend on the regulatory factors present in the system, and are different under basal, TGF- β (10 ng/ml), and IL-1 (10 ng/ml)

conditions. IL-1 downregulates PRG4 secretion by chondrocytes from 2.89×10^{-7} mg/(cm²·s) to 1.16×10^{-7} mg/(cm²·s), while TGF- β upregulates PRG4 secretion to 1.16×10^{-6} mg/(cm²·s) (Flannery *et al.*, 1999; Schmidt *et al.*, 2005). Synoviocyte PRG4 secretion is similarly regulated by these cytokines, as IL-1 downregulates secretion from 4.05×10^{-9} mg/(cm²·s) to 2.43×10^{-9} mg/(cm²·s), and TGF- β upregulates secretion to 2.23×10^{-8} mg/(cm²·s) (unpublished data). TGF- β and IL-1 result in increased HA secretion by synoviocytes, rising from 2.84×10^{-9} mg/(cm²·s) to 6.72×10^{-8} mg/(cm²·s) and 9.95×10^{-8} mg/(cm²·s), respectively (Haubeck *et al.*, 1995). Cellular secretion rates for synoviocytes were converted to tissue secretion rates using a ~ 0.8 surface area fraction of synovium occupied by synoviocytes (Price *et al.*, 1995) and assuming a typical cell diameter of ~ 16 μ m.

Solutions

Using the parameter values above and listed in Table 2, the first-order system of ordinary differential equations were solved numerically using Matlab 7.0 (The MathWorks, Natick, MA). Results are given for both the low and high end of the predicted concentration range for each lubricant. General concentration profiles are also presented as a function of the non-dimensional constants and τ_i .

Table 2 Values used in the model. TGF- β and IL-1 values are for a concentration of 10 ng/ml.

Variable	Units	Value (basal)	(TGF- β)	(IL-1)	References
D_{HA}	cm ² /s	9.80×10^{-8}			Lu, 2005
D_{PRG4}	cm ² /s	1.11×10^{-7}			Swann, 1981
r_{HA}^{SYN}	mg/(cm ² ·s)	2.84×10^{-9}	6.72×10^{-8}	9.95×10^{-8}	Haubeck, 1995
r_{PRG4}^{AC}	mg/(cm ² ·s)	2.89×10^{-7}	1.16×10^{-6}	1.16×10^{-7}	Schmidt, 2005
r_{PRG4}^{SYN}	mg/(cm ² ·s)	4.05×10^{-9}	2.23×10^{-8}	2.43×10^{-9}	unpublished data
A^{AC}	cm ²	121			Eckstein, 2001
A^{SYN}	cm ²	277			Davies, 1946
V^{SF}	ml	1.1			Ropes, 1940
L	cm	0.005			Price, 1995
θ_{cell}		0.42-0.67			Levick, 1989a,b
θ_{col}		0.2			Levick, 1994
θ_{GAG}		0.0075			Sabaratnam, 2005
					Scott, 2003
ζ_{col}		0.7			Maroudas, 1970, Sullivan, 1942
ζ_{cell}		0.69			Levick, 1989a,b
a_{GAG}	nm	0.56			Ogston, 1973
ρ_{HA}	g/ml	1.45			Mahlbacher, 1992 Mason, 1982
ρ_{PRG4}	g/ml	1.45			Swann, 1981
MW_{HA}	kDa	2000-6000			Fraser, 1997
MW_{PRG4}	kDa	220-345			Swann, 1977 Schumacher, 1994

Results

Case 1: Steady-state Lubricant Composition

The form of the solution for c_i^{SF} at steady-state is determined from equations 13-18,

$$c_i^{SF}(t = \infty, \alpha) = c_{i,basal}^{SF} \left\{ k_1 \cdot \frac{r_i^{SYN}(\alpha)}{r_{i,basal}^{SYN}} + k_2 \cdot \frac{r_i^{AC}(\alpha)}{r_{i,basal}^{AC}} \right\} \quad (30)$$

or equivalently, from equations 1 and 4:

$$c_i^{SF}(t = \infty, \alpha) = \frac{r_i^{SYN}(\alpha) + r_i^{AC}(\alpha) \cdot \frac{A^{AC}}{A^{SYN}}}{p_i^{SYN}} \quad (31)$$

The form of the equations shows that increases in r_i^{AC} and r_i^{SYN} result in increases in c_i^{SF} . Increases in k_1 and k_2 also cause increases in c_i^{SF} , and can be achieved by decreases in p_i^{SYN} or increases in the ratio of A^{AC} to A^{SYN} .

A range of values has been noted for some of the parameters used in the model (Table 2), and thus there was a range of model predictions for lubricant concentrations in SF. Permeability ranged from 6.79×10^{-7} cm/s - 1.56×10^{-6} cm/s for PRG4 and 1.73×10^{-8} cm/s - 1.84×10^{-7} cm/s for HA. The range of predictions for c_{PRG4}^{SF} and c_{HA}^{SF} at steady-state under basal conditions was 0.08-0.19 mg/ml and 0.02-0.16 mg/ml, respectively. With TGF- β stimulation, c_{PRG4}^{SF} increased to 0.34-0.77 mg/ml and c_{HA}^{SF} increased to 0.36-3.89 mg/ml, while with IL-1 c_{PRG4}^{SF} decreased to 0.03-0.08 mg/ml but c_{HA}^{SF} increased to 0.54-5.77 mg/ml (Table 3).

Transient Changes in Lubricant Composition

The form of the solution for transient changes in c_i^{SF} is determined from equations 13-18,

$$\frac{\partial c_i^{SF}(\alpha, t)}{\partial t} = \frac{c_{i,basal}^{SF}}{\tau_i} \left\{ k_1 \frac{r_i^{SYN}(\alpha)}{r_{i,basal}^{SYN}} + k_2 \frac{r_i^{AC}(\alpha)}{r_{i,basal}^{AC}} - \frac{c_i^{SF}(\alpha, t)}{c_{i,basal}^{SF}} \right\} \quad (32)$$

or equivalently, from equations 1 and 4:

$$\frac{\partial c_i^{SF}(\alpha, t)}{\partial t} = \frac{r_i^{SYN}(\alpha) \cdot A^{SYN} + r_i^{AC}(\alpha) \cdot A^{AC} - p_i^{SYN} \cdot c_i^{SF}(\alpha, t) \cdot A^{SYN}}{V^{SF}} \quad (33)$$

General curves with concentration plotted against time for conditions of joint lavage and HA injection are shown in Figure 3. This general case illustrates that steady state lubricant concentration levels are governed by the non-dimensional constants k_1 and k_2 and secretion rates, while the temporal effects are governed by τ_i . The parameter τ_i

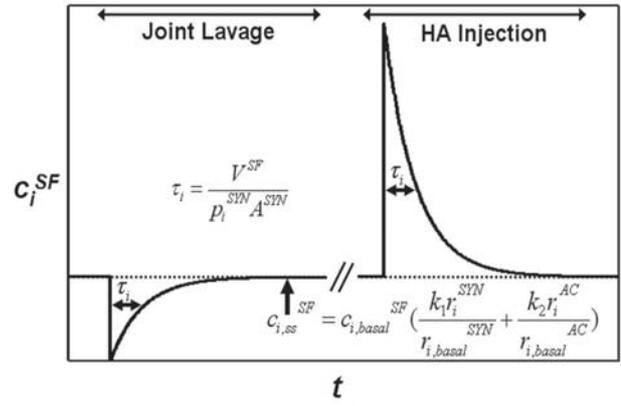


Figure 3. General curves of concentration plotted against time for conditions of joint lavage and HA injection, illustrating that steady state lubricant concentration levels are governed by the non-dimensional constants k_1 and k_2 and secretion rates, while the temporal effects are governed by τ_i .

describes the kinetics of lubricant concentration in SF, and represents the time to reach 63% of the steady state concentration after joint lavage, or time for 63% of injected HA to be cleared from the SF. The form of τ_i shows that increases in p_i^{SYN} and A^{SYN} result in decreases in τ_i , while increases in V^{SF} cause increases in τ_i . Numerical values for transient and steady state lubricant concentrations in the different cases are discussed below.

Case 2: Joint Lavage

After joint lavage, the starting concentration of lubricants in SF was decreased in a step-wise manner to 0 mg/ml at $t=0$ and returned to the predicted steady-state concentration with kinetics that were markedly different for PRG4 and HA. The range of time constants, which indicate the time to reach 63% of steady-state concentration of lubricant in SF were 0.03-0.07 days for PRG4 (Fig. 4a,b) and 0.25-2.66 days for HA (Fig. 4c,d). Chemical stimulation with TGF- β and IL-1 is not predicted to alter the kinetics of lubricant restoration following joint lavage; however, as noted for steady-state predictions, TGF- β and IL-1 dictated the magnitude attained at steady-state.

Case 3: Therapeutic HA Injection

After an HA injection of 20 mg, the concentration of HA in SF increased by 18.2 mg/ml and then returned to steady-state concentration after a duration of time (Fig. 5a,b). The time for 63% of the injected HA to be cleared from the joint, was 0.25-2.66 days. As stated above, chemical stimulation with TGF- β and IL-1 did not alter the kinetics associated with HA injection, but dictated the magnitude of the final steady-state concentration.

Discussion

This study describes some essential features of steady-state and kinetic SF lubricant composition in whole joints under normal or altered chemical environments, and also with different therapeutic interventions. The model predicts steady-state lubricant concentrations that are consistent

Table 3. Steady-state model predictions of ranges of synovial fluid lubricant composition under basal conditions or with 10 ng/ml of TGF- β or IL-1.

Condition		Concentration range [mg/ml]	
		PRG4	HA
Predicted	physiological	0.05 – 0.35	1 – 4
	basal	0.08 – 0.19	0.02 – 0.16
	TGF- β	0.34 – 0.77	0.36 – 3.89
	IL-1	0.03 – 0.08	0.54 – 5.77

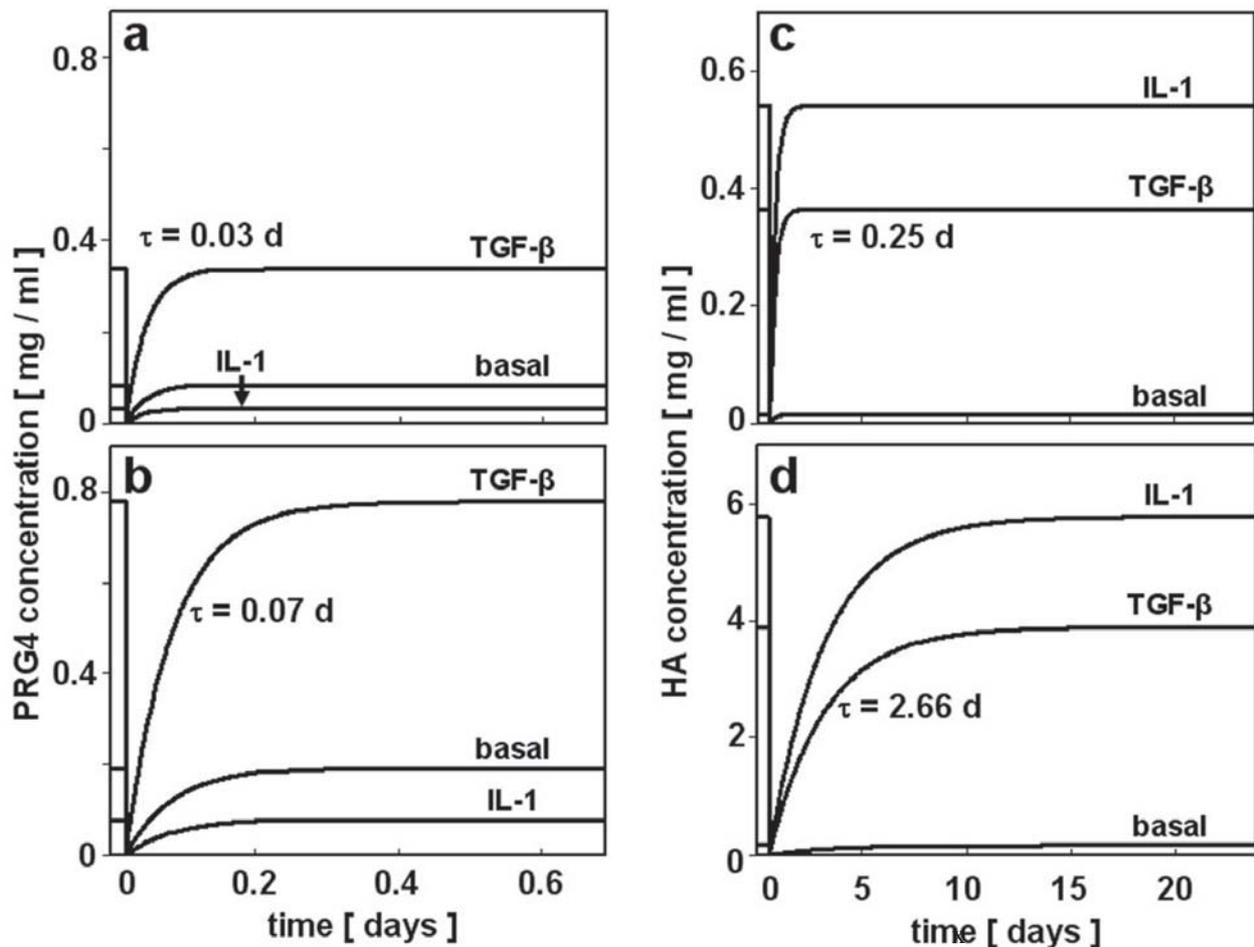


Figure 4. Transient rise in synovial fluid lubricant concentration after joint lavage, with or without chemical regulatory factors, and associated time constants, τ . (a) low end PRG4 predictions, (b) high end PRG4 predictions, (c) low end HA predictions, and (d) high end HA predictions.

with physiologically observed concentrations. Further, chemical alterations in the synovial joint environment that may occur in injury and disease were predicted to alter lubricant concentration. The kinetics associated with joint lavage predicted that PRG4 and HA achieve steady-state concentration on distinct time scales. Finally, therapeutic injection of HA into SF was predicted to cause an immediate increase in HA concentration, which returns to steady-state concentration after ~ 1 -2 days.

The quantitative intercompartmental model developed in this study included several assumptions that allowed for a straightforward analysis that could be expanded upon. For example, the model could be extended by including additional environmental factors and allowing a number of parameters to change with the environment and time. Some parameters in the model are also described in bulk and spatially averaged terms rather than on multiple scale levels. Finally, physical and chemical interactions of lubricants with their environment were not considered in the model, and may affect the free concentration of lubricants in SF.

While lubricant secretion rates were the sole variables in the model that were assumed to be dependent on chemical factors, other variables and parameters included in the model may also be affected by these and other

environmental factors. Such environmental factors can include mechanical stimuli that are also known to regulate lubricant secretion by both chondrocytes and synoviocytes. Compressive forces downregulate PRG4 secretion by chondrocytes, while shear forces upregulate PRG4 secretion (Nugent *et al.*, 2006a; Nugent *et al.*, 2006b). Mechanical stretching of synovium results in increased HA secretion by synoviocytes (Mombberger *et al.*, 2005). Both chemical and mechanical factors may affect not only lubricant secretion, but also parameters that influence permeability of the synovial membrane. For example, different cytokines may have anabolic or catabolic effects on the extracellular matrix of synovium and thus alter its composition and organization. The increased permeability of the synovium in rheumatoid arthritis may possibly reflect such a phenomenon (Levick, 1981). Joint motion involving stretching of the synovium may result in changes in thickness and area of the membrane, leading to altered permeability. Chemical and mechanical factors may also affect synovium permeability by regulating aspects of lubricant metabolism, such as the molecular weight form of lubricant that is secreted. In the SF of arthritic joints, HA exists at a lower molecular weight (Balazs, 1980; Dahl *et al.*, 1985), while in normal SF, PRG4 may exist in both monomeric and multimeric forms (Plaas *et al.*, 2006).

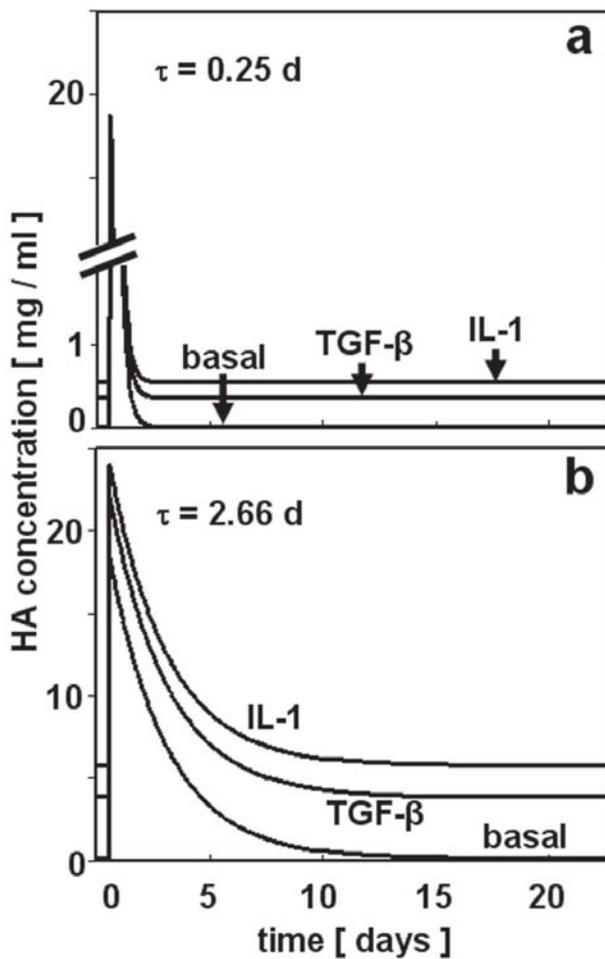


Figure 5. Transient changes in synovial fluid lubricant concentration after therapeutic HA injection, with or without chemical regulatory factors, and associated time constants, τ . (a) low end HA predictions and (b) high end HA predictions.

Changes in any of these parameters that affect permeability to lubricants may also alter the rate at which fluid is transported across the synovial membrane. The direction, i.e. entry or exit, of this fluid transport may similarly be controlled by chemical and mechanical factors, such as osmotic pressure exerted by SF molecules and hydrostatic pressure due to joint flexion and extension. Thus, changes in parameters that affect permeability may subsequently lead to changes in SF volume. Such concomitant alterations in membrane area and permeability, SF volume, and the turnover of SF are observed in cases of joint swelling associated with injury or disease (Levick, 1990; Wallis *et al.*, 1987).

The parameters of the compartmental model may be taken as a macroscopic representation of processes occurring on multiple scales, each of which may have distinct spatial and temporal characteristics. For example, the matrix composition of the synovium may be affected by cytokines that alter the content of a specific collagen type. The current model reflects this change only in the lumped parameters that represent total collagen volume fraction and tortuosity, and thus does not attempt to

discriminate details on this scale. The model also does not reflect alterations in gene expression for either lumped or specific components. At each of these scales, tissue properties may vary throughout the total area or volume, and triggered events may occur over distinct time scales for different components.

Interactions of lubricants with themselves, other lubricants, or with surrounding tissues could also be included in the model. For example, PRG4 may interact with itself, as both monomeric and multimeric forms have been observed (Plaas *et al.*, 2006). HA may also be influenced by its own presence, as secretion by synoviocytes can depend upon the concentration and molecular weight form of HA in the environment of the synoviocytes (Smith and Ghosh, 1987). Lubricant molecules may also interact with each other. In particular, the putative lubricant surface active phospholipid (SAPL) may bind to HA or PRG4 and be carried in SF by these molecules (Hills, 2000). It should be noted that SAPL was not examined in this model as there is conflicting evidence on its role in joint lubrication (Hills and Crawford, 2003; Jay and Cha, 1999). However, its behaviour indicates that interactions between molecules in SF do exist. Electrostatic interactions between lubricants and the extracellular matrix of synovium, and binding of lubricants to tissues in the joint may also be important processes affecting SF lubricant composition.

Steady-state lubricant concentrations predicted by the model were generally consistent with those observed physiologically. The concentration of PRG4 in human SF ranges from 52-350 $\mu\text{g/ml}$ in normal joints post-mortem, and increases to 276-762 $\mu\text{g/ml}$ in SF obtained from patients undergoing arthrocentesis procedures (Schmid *et al.*, 2001a). In acute injury in a rabbit knee model, PRG4 concentration decreased from 280 $\mu\text{g/ml}$ to 20-100 $\mu\text{g/ml}$ (Elsaid *et al.*, 2005). Model predictions of c_{PRG4}^{SF} at steady-state under basal conditions were comparable to that observed in normal SF *in vivo*. The model predicted an increased PRG4 concentration with TGF- β stimulation but decreased concentration with IL-1, which may reflect distinct changes in the SF chemical environment that occur with different types of injury and disease. The concentration of HA in human SF ranges from 1-4 mg/ml in healthy individuals (Balazs, 1974; Chmiel and Walitza, 1980; Mazzucco *et al.*, 2004; Watterson and Esdaile, 2000), and decreases after effusive joint injury (Asari *et al.*, 1994) and in arthritic disease to ~ 0.1 -1.3 mg/ml (Dahl *et al.*, 1985; Mazzucco *et al.*, 2004). Model predictions of c_{HA}^{SF} under basal conditions were considerably below normal SF concentration. Stimulation with either TGF- β or IL-1 increased c_{HA}^{SF} to the upper range of *in vivo* levels, which may indicate that a certain concentration of these cytokines is required in normal SF to achieve physiological concentrations of HA. The discrepancy between observed HA concentration in diseased joints and model predictions in an environment of increased cytokine concentration that may exist in injury and disease might result from allowing only lubricant secretion rates in the model to change as a function of the environment. As discussed previously, chemical stimuli may exert their effects on SF lubricant

composition by altering the permeability of the synovium which may dominate over alterations in lubricant secretion rates.

The distinct kinetics of PRG4 and HA restoration after joint lavage have implications for disease and clinical therapies. For example, in acute injury, both PRG4 and HA concentrations are observed to decrease (Asari *et al.*, 1994; Elsaid *et al.*, 2005). Model predictions suggest that after the inflammation of an acute injury has cleared, the concentration of PRG4 may be restored relatively rapidly compared to the concentration of HA. The minimum concentration of lubricants in SF that is required to create a mechanically functional fluid is unknown. However, decreasing doses of SF and the PRG4 and HA constituents results in increased friction between articulating cartilage surfaces in a cartilage-on-cartilage friction test (Schmidt *et al.*, 2007). If the joint lavage procedure challenges the low-friction, low-wear environment of synovial joints in the short term, it may prove beneficial to provide adjunctive therapies to normalize lubricant concentrations. Steroid supplementation is commonly given with joint lavage to help reduce inflammation (Frias *et al.*, 2004; Tanaka *et al.*, 2006), and more recently, HA supplementation has been given to enhance lubrication in the joint and decrease post-procedure pain (Mathies, 2006). The model predictions in this study support the use of lubricant supplementation to temporarily increase lubricant concentration in SF.

The clearance rate of HA predicted by the model after therapeutic injection is generally consistent with experimental reports, suggesting that this approach of analysis may be useful for putative therapies involving delivery of PRG4. The half-life of HA in SF has been studied in rabbit and sheep models, and is on the order of ~24 hours for normal joints (Coleman *et al.*, 1997; Laurent *et al.*, 1992; Sakamoto *et al.*, 1984), but decreases to ~12 hours in the case of induced arthritis in the sheep model (Fraser *et al.*, 1993). In the present study, simulated therapeutic delivery of HA into SF resulted in a large instantaneous rise in concentration over the steady-state levels, but the model predicted that the injected HA appreciably cleared (i.e. 63% cleared) after 0.25-2.66 days. This rate of clearance is also consistent with the periodic weekly injection of HA into diseased joints (Tehranzadeh *et al.*, 2005). Clinical results of therapeutic HA injection can be highly dependent upon the molecular weight of HA (Ghosh and Guidolin, 2002; Moreland, 2003), possibly reflecting changes in synovium permeability and the half-life of this molecule in SF. Thus, the present model may have applications in comparing the kinetics of molecular concentrations with associated clinical outcomes.

The quantitative intercompartmental model of SF lubricant composition developed in this study may also have applications to a variety of current and future joint therapies. In partial or total knee arthroplasty, removal of the cartilage surface areas may affect lubricant concentration. In cell injection or transplantation therapies, the model may elucidate the effects of the cell sources on lubricant concentration. In engineering whole biological joints, the model may facilitate development of a mechanically functional bioengineered SF in a closed

volume. Such bioengineering of fluid, as opposed to the traditional engineering of tissues, may be a critical component of a whole joint bioreactor system for creation of large contoured orthotopic tissue blocks for biological arthroplasty.

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Discussion with reviewers

C Flannery: It would be interesting to consider further the proportion of the total PRG4/lubricin in a joint that occurs localized to tissue surfaces (i.e. cartilage).

Authors: This proportion can be estimated as follows. The amount of PRG4 bound to the surface of bovine cartilage is $\sim 0.24\text{--}0.59 \mu\text{g}/\text{cm}^2$ (Schmidt *et al.*, 2005; Nugent *et al.*, 2006). Using parameter values from the present manuscript, a joint with 140 cm^2 cartilage surface area (Eckstein *et al.*, 2001) would have a total of $\sim 34\text{--}83 \mu\text{g}$ bound PRG4. In synovial fluid, the PRG4 concentration is $450 \mu\text{g}/\text{ml}$ (Schmid *et al.*, 2001). Assuming a synovial fluid volume of 1.1 ml (Ropes *et al.*, 1940) yields a total of $\sim 500 \mu\text{g}$ PRG4 in synovial fluid. From these estimates, the proportion of total PRG4 that is bound to the articular cartilage surface would be $\sim 7\text{--}17\%$.

C Flannery: It would be interesting to consider further whether/how this parameter is affected by relative changes in the lubricant composition of the synovial fluid compartment.

Authors: The proportion of PRG4 that is bound may be affected as suggested. The binding of synovial fluid PRG4 to cartilage surfaces occurs in a dose-dependent manner (Swann *et al.*, 1981), and repletion of PRG4 that has been removed from the surface of cartilage is dependent upon the structure of the PRG4 protein (Jones *et al.*, 2006; Nugent *et al.*, 2006).

C Flannery: Are there any alterations to the levels of such boundary-associated molecules which could be predicted for the example cases of joint lavage and HA injection?

Authors: In the case of joint lavage, where the synovial fluid concentration of lubricants is initially brought to \sim zero, PRG4 may be expected to be desorbed or released due to chemical or mechanical factors. The significance of this depletion may depend upon the rate at which it

occurs. Rapid depletion may be detrimental to joint lubrication, while slow depletion may be compensated by *de novo* PRG4 secretion. A similar hypothesis may apply for HA after joint lavage, with differing kinetics. In the case of HA injection, where the HA concentration is transiently increased, HA binding may be expected to increase, possibly in a saturable manner.

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